

Frequency Angular Sounding (FAS) Technique



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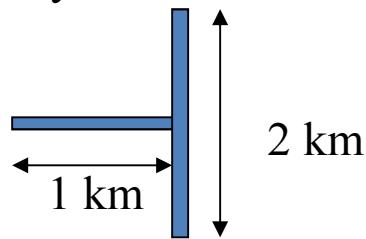
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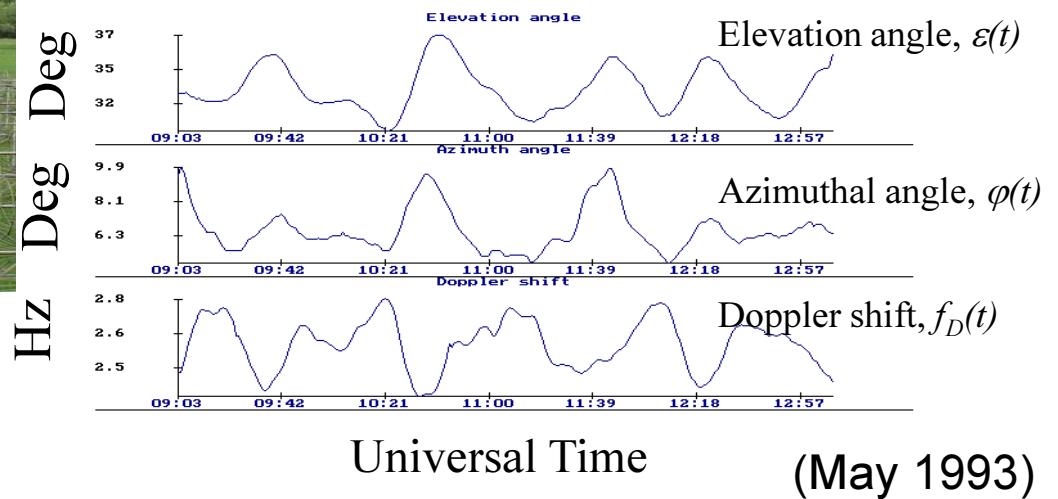
UTR-2 Phased Array



Array Dimensions



Example of oblique signal trajectory parameters (700 km radio path)



∴ Signals from HF broadcasting or time-service stations can be used for monitoring TIDs.

FAS principles

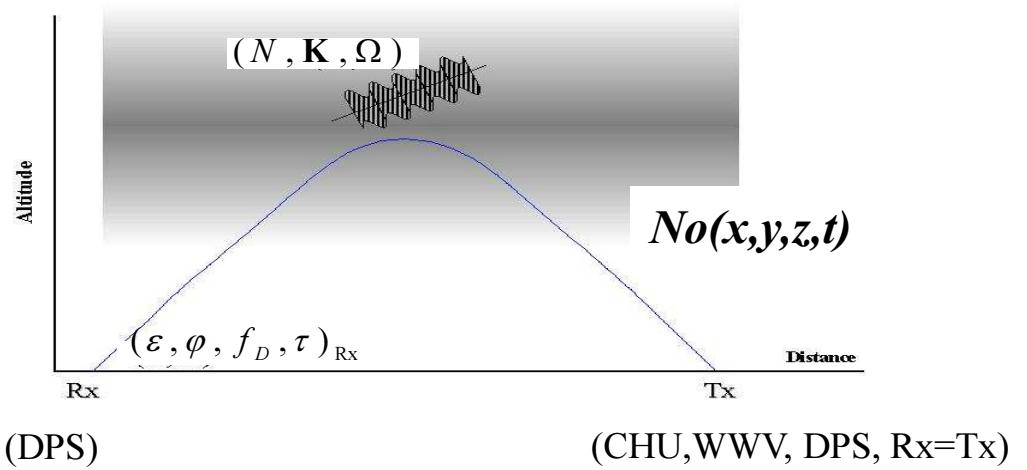
Measured signal parameters:

$\varepsilon(t)$ elevation angle

$\varphi(t)$ azimuthal angle

$f_D(t)$ Doppler shift

$\tau(t)$ Signal delay (vert. sound.)



Direct problem: $(N, K, \Omega) \Rightarrow (\varepsilon, \varphi, f_D, \tau)_\text{Rx}$

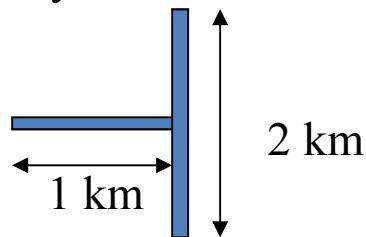
Inverse problem: $(\varepsilon, \varphi, f_D, \tau)_\text{Rx} \Rightarrow (N, K, \Omega)$

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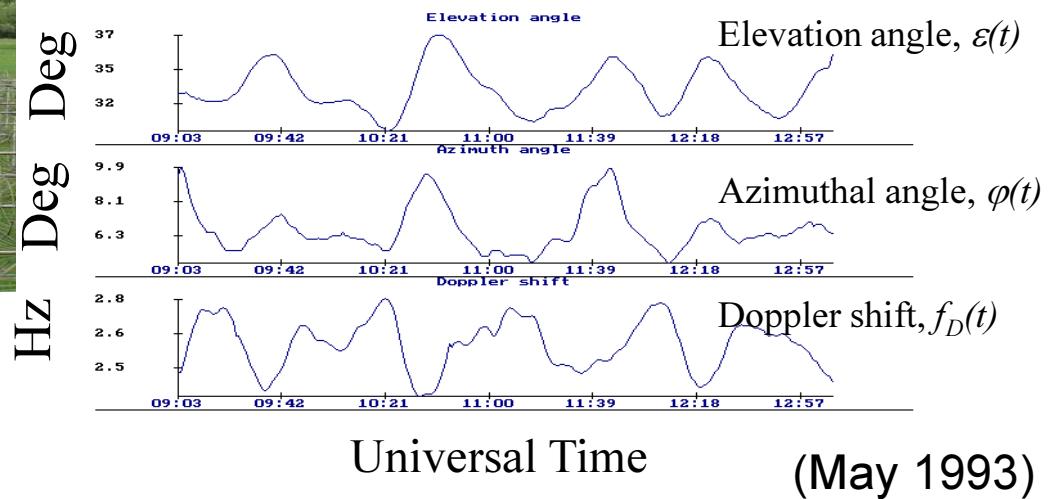
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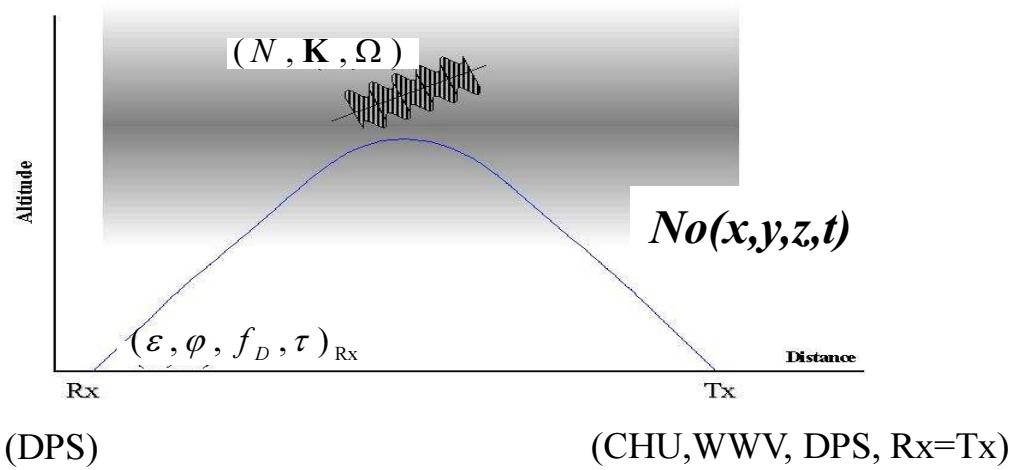
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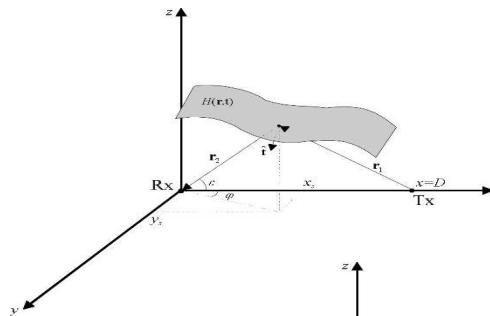


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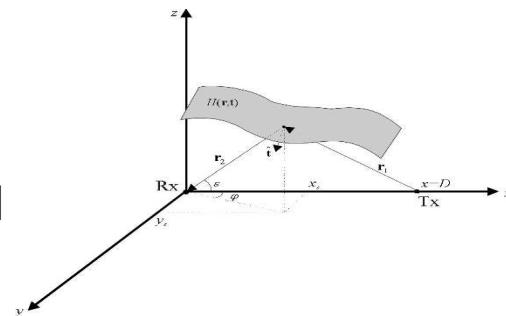
FAS: 3 approaches

1. Oblique



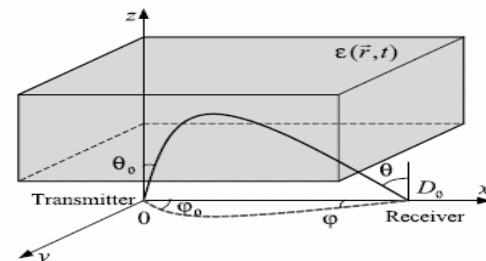
Perfectly reflecting surface is assumed.
 $Tx \neq Rx$

2. Vertical/Generalized

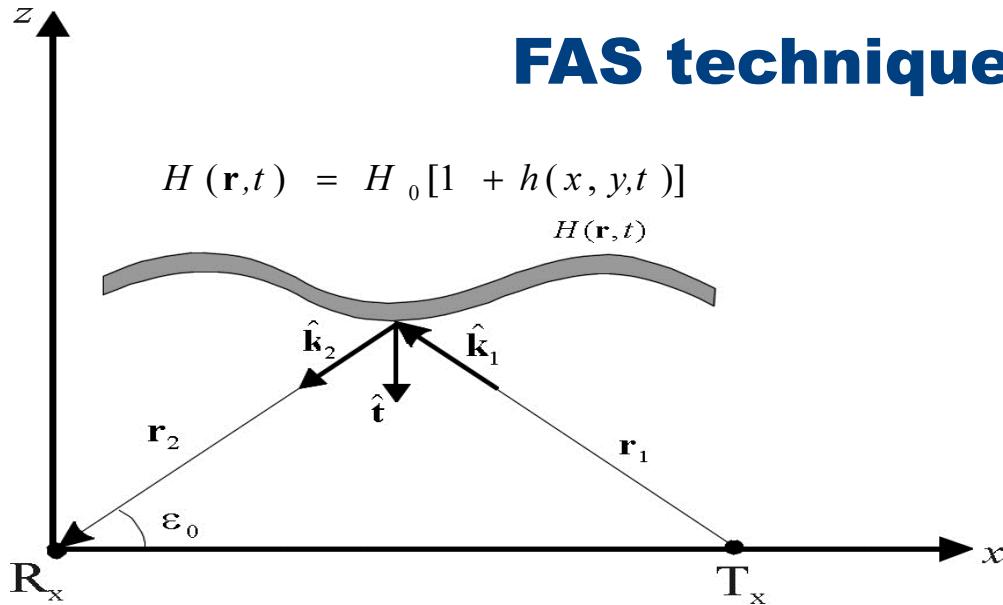


Perfectly reflecting surface is assumed.
Vertical case is ok

3. “3D density waves”



Ionospheric layer is assumed.
 $Tx \neq Rx$



FAS technique: approach

$$H(\mathbf{r},t) = H_0[1 + h(x,y,t)]$$

$$H(\mathbf{r},t)$$

$$\hat{\mathbf{k}}_2$$

$$\hat{\mathbf{k}}_1$$

$$\hat{\mathbf{t}}$$

$$\mathbf{r}_2$$

$$\mathbf{r}_1$$

Perfectly reflecting surface model

Surface spectral representation:

$$h(x,y,t) = \int_{-\infty}^{\infty} N(\Omega) e^{i\Omega t} d\Omega e^{-iK(\Omega)(x \cos \theta(\Omega) + y \sin \theta(\Omega))}$$

$N(\Omega)$ – TID amplitude

$K(\Omega)$ – TID wavenumber

$\theta(\Omega)$ – TID direction of motion

Measured signal parameters:

$\varepsilon(t)$ elevation angle

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$f_D(t)$ Doppler shift

Spectral representations:

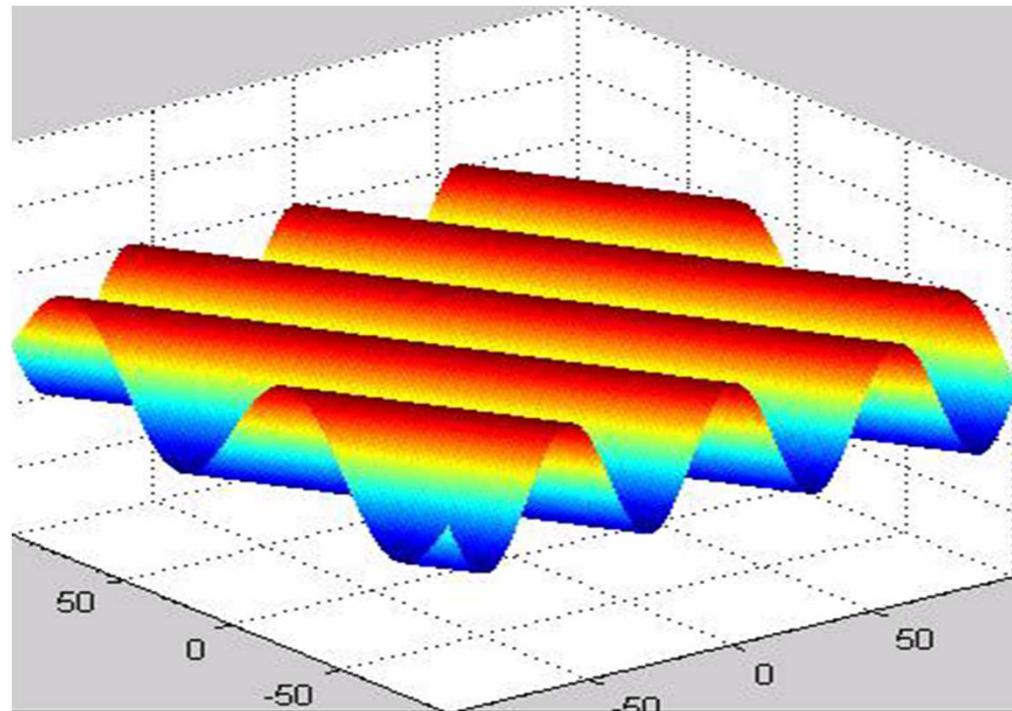
$$\varepsilon(t) = \int_{-\infty}^{\infty} S_{\varepsilon}(\Omega) e^{i\Omega t} d\Omega$$

$$\varphi(t) = \int_{-\infty}^{\infty} S_{\varphi}(\Omega) e^{i\Omega t} d\Omega$$

$$f_D(t) = \int_{-\infty}^{\infty} S_F(\Omega) e^{i\Omega t} d\Omega$$

$$\boxed{\varepsilon(t), \varphi(t), f_D(t) \Leftrightarrow h(x,y,t)}$$

Surface model visualization



Oblique FAS: cont.

With the use of the spectral representation, one gets solutions

Trajectory parameters spectra: (direct problem)

$$S_\varepsilon(\Omega) = N(\Omega)[\sin \varepsilon_0 \cos \varepsilon_0 - iH_0 K(\Omega) \cos \theta(\Omega)]$$

$$S_\varphi(\Omega) = iH_0 K(\Omega) N(\Omega) \tan \varepsilon_0 \sin \theta(\Omega)$$

$$S_F(\Omega) = -2iH_0 \Omega N(\Omega) \sin \varepsilon_0 / \lambda$$

Reflecting surface spectra: (inverse problem)

$$N(\Omega) = \frac{i\lambda S_F(\Omega)}{2H_0 \Omega \sin \varepsilon_0}$$

$$\tan \theta(\Omega) = -\frac{2H_0 \Omega \operatorname{Re} S_\varphi(\Omega)}{2H_0 \Omega \operatorname{Re} S_\varepsilon(\Omega) \tan \varepsilon_0 + \lambda \operatorname{Im} S_F(\Omega) \sin \varepsilon_0}$$

$$K(\Omega) = -\frac{2\Omega \operatorname{Im} S_\varphi(\Omega) \cos \varepsilon_0}{\lambda \operatorname{Im} S_F(\Omega) \sin \theta(\Omega)}$$

Measurements with FAS technique

Comparing TIDs parameters measured with DPS and ISR.

Date	Digisonde FAS			ISR		
	Velocity, m/s	Wavelength, km	Azimuth, deg	Velocity, m/s	Wavelength, km	Azimuth, deg
15.03.2001	341	655	117	305	585	102
16.03.2001	135	258	-80	156	274	-82

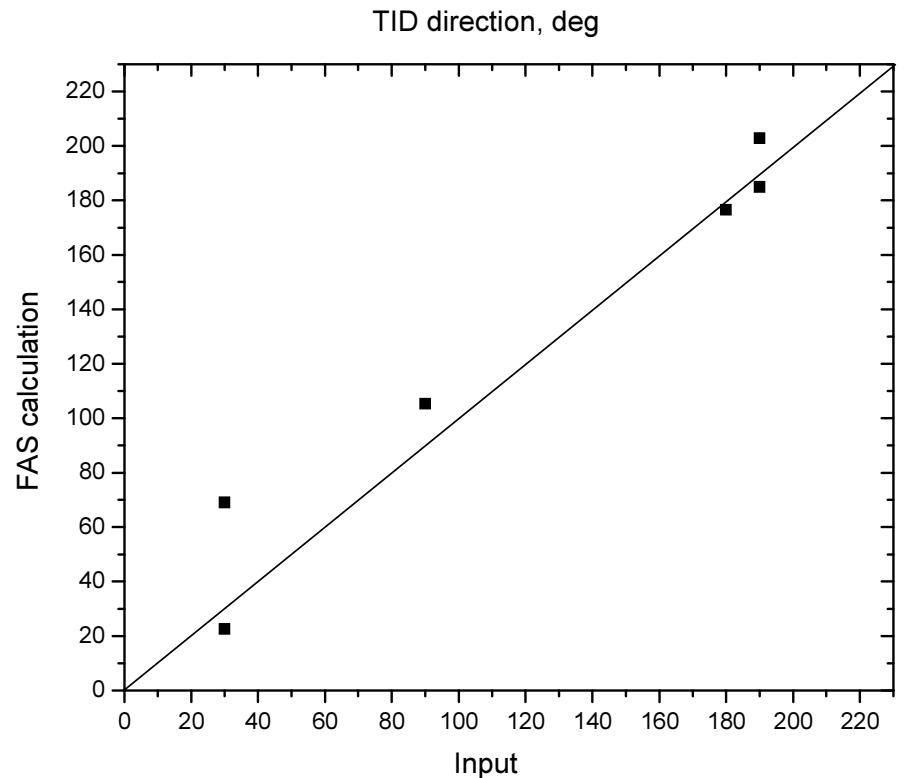
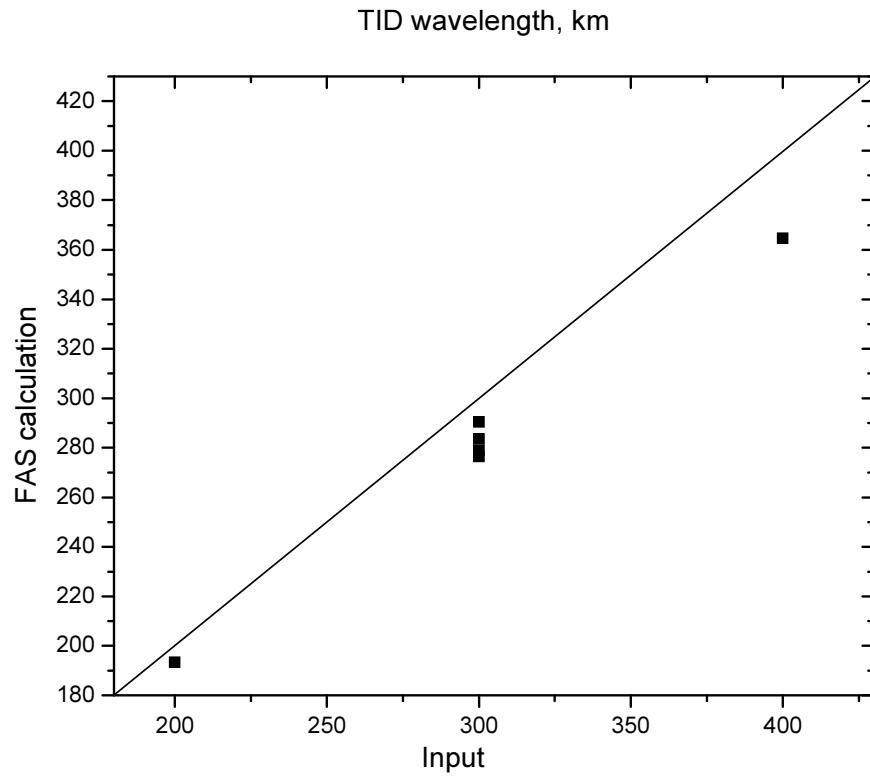
Comparison of the 30 min TID parameters obtained with FAS and ISR techniques for March 15, 2001 data

	Velocity, m/s	Wavelength, km	Propagation direction, deg	Amplitude,
ISR data	305	585	102	2.0 %
FAS (surface)	341	655	117	0.8 %
FAS (bottom)	217	610	115	1.0 %

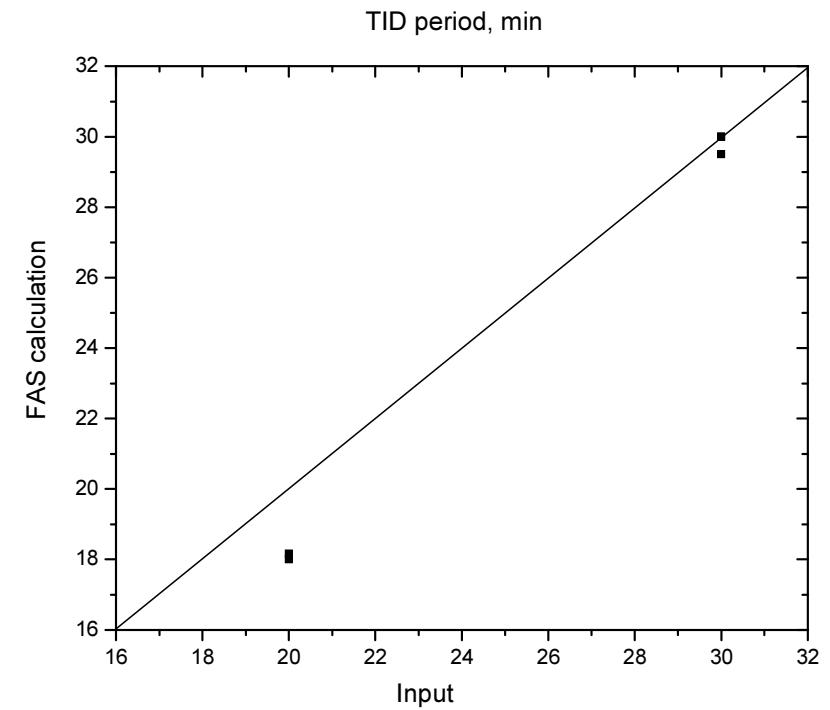
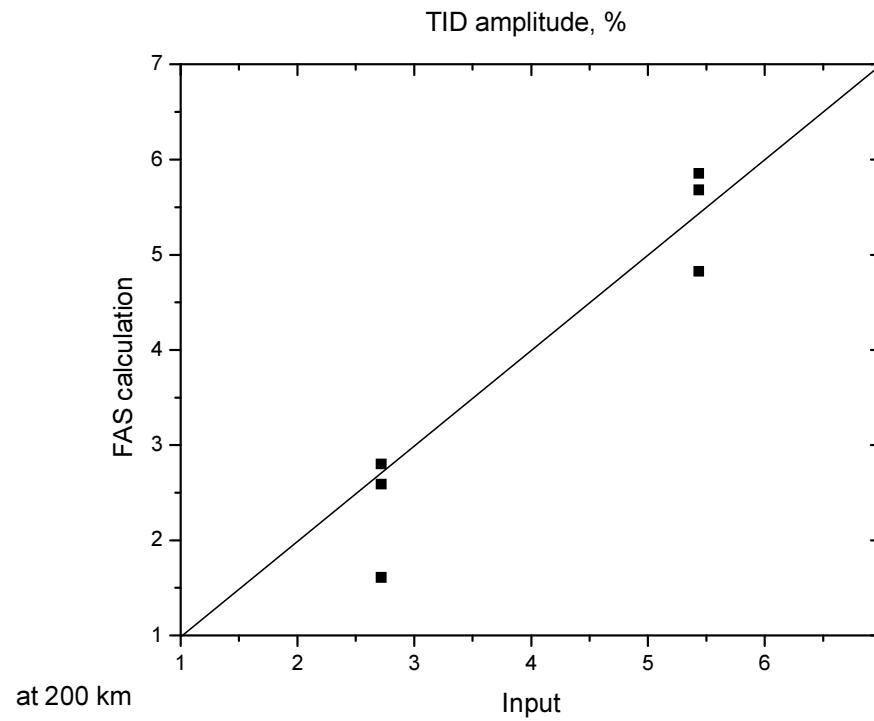
Simulation runs to test FAS accuracy

	Run1	Run2	Run3	Run4	Run5	Run6
Propagation						
fo, MHz	8.0	8.0	5.0	5.0	5.0	6.0
UT	17:00	17:00	5:00	5:00	5:00	7:00
Distance, km	324	651	651	651	651	853
TID parameters						
Period, min	30	30	30	30	20	30
Wavelength,k m	300	300	300	400	200	300
Direction, deg	180	30	90	190	190	30
Amplitude, A	0.01	0.02	0.02	0.01	0.01	0.02

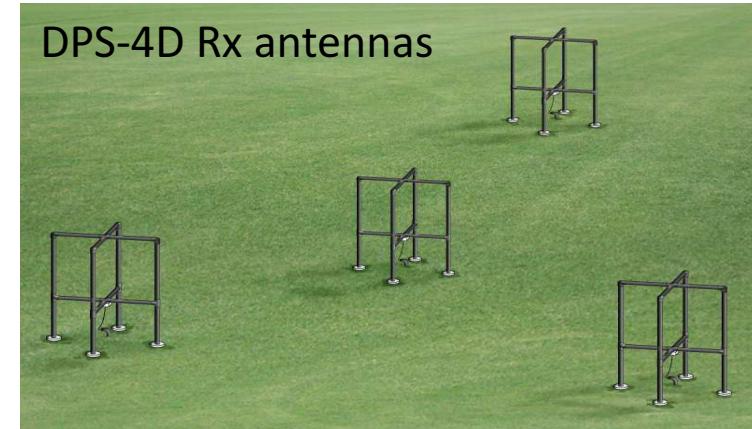
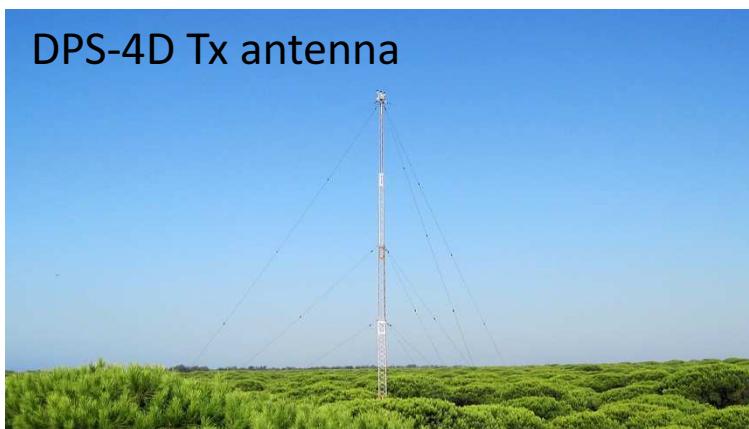
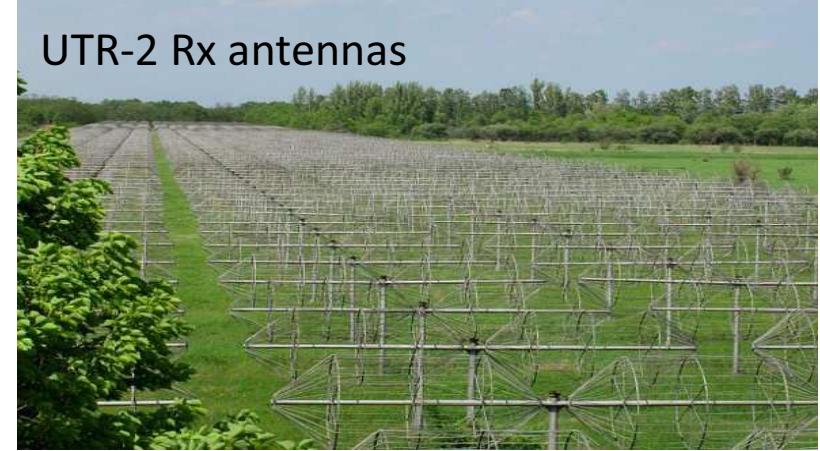
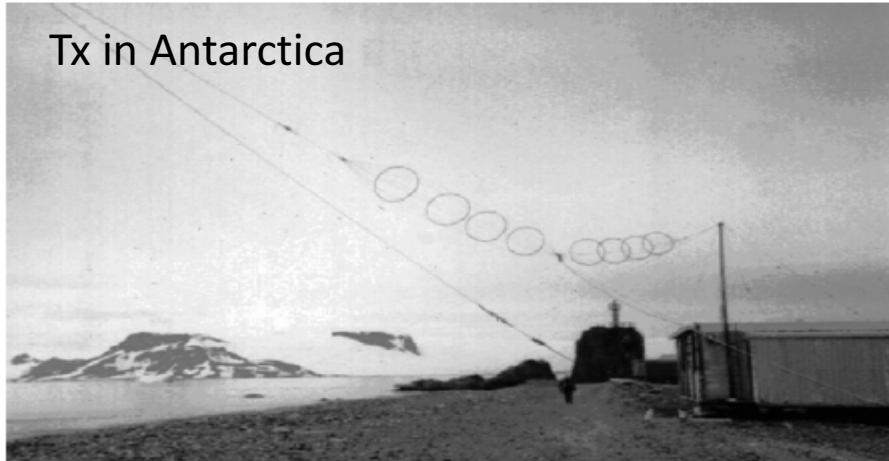
FAS accuracy test results



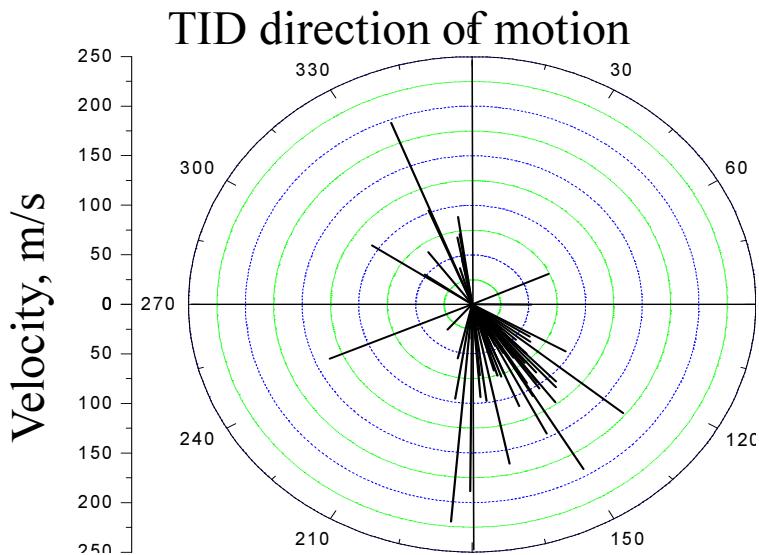
FAS accuracy test results (cont)



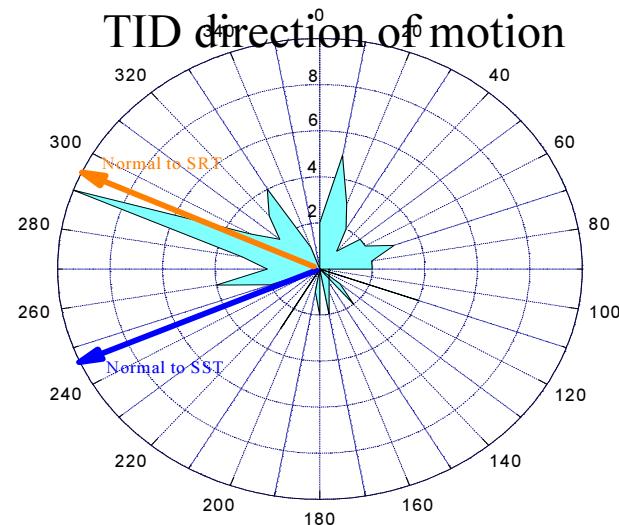
Experimental setups



Measurements with FAS technique



Millstone Hill, November 2003
(geomagnetically disturbed period)



Antarctica, Feb-Mar 2004
(quiet period)

Histogram of TID azimuths. The orange and blue arrows are along the normal to the sunrise (SRT) and sunset (SST) terminators, respectively.

FAS requirements

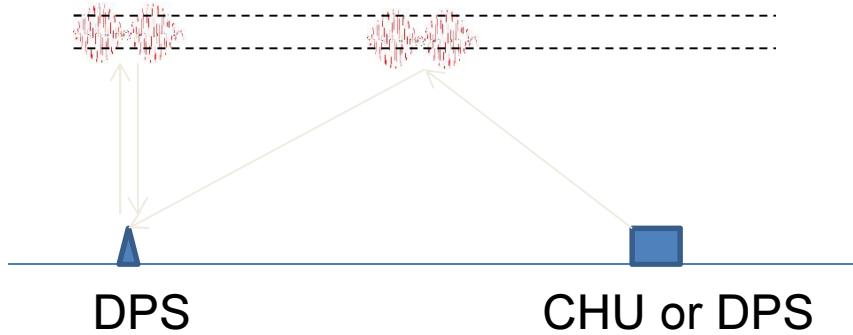
To measure continuously:

$\alpha(t)$ elevation angle

$\varphi(t)$ azimuthal angle

$f_D(t)$ Doppler shift

$\tau(t)$ Signal delay (vert. sound.)



Approximately:

Angles of arrival accuracy: $\sim 1^\circ$

Spectral resolution: 0.03-0.1Hz

Data taking rate: 1..10 min

Frequency stability: $\sim 10^{-9}$ (for oblique sounding)

Conclusions and Recommendations

FS technique is capable of measuring TID parameters

FAS technique accuracy is about 10%

FAS technique can be integrated into DPS-4D systems.

We propose to establish Rapid-TID system of TID monitoring based on the FAS technique

Dalu
감사합니다

Gracias Danke Ευχαριστίες

THANK YOU

Obrigado
Köszönöm

Tack
ありがとう

Grazie
Спасибо Dank

謝謝 Merci

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